ECE334 Digital Electronics Equation Sheet

Constants: $k = 1.38 \times 10^{-23}\,\mathrm{JK}^{-1}$; $q = 1.602 \times 10^{-19}$ C ; $V_T = kT/q \approx 26\,\mathrm{mV}$ at 300 °K ;
$\varepsilon_0 = 8.854 \times 10^{-12}$ F/m ; $k_{ox} = 3.9$; **caps:** $C_{ox} = (k_{ox}\varepsilon_0)/t_{ox}$; $C_j = C_{j0}/(1 + V_R/\phi_0)^{M_j}$;

NMOS: $\beta_n = \mu_n C_{ox}(W/L)$; $V_{tn} > 0$; $V_{DS} \geq 0$; (triode) $I_D = \beta_n((V_{GS} - V_{tn})V_{DS} - (V_{DS}^2/2))$; (active) $I_D = 0.5\beta_n(V_{GS} - V_{tn})^2$;
(triode) $V_{DS} \leq (V_{GS} - V_{tn})$; (active) $V_{DS} \geq (V_{GS} - V_{tn})$; $V_{tn} = V_{tn0} + \gamma(\sqrt{V_{SB} + \phi_s} - \sqrt{\phi_s})$;
(subthreshold) $I_D = I_{D0} e^{((V_{GS} - V_{tn})/(nV_T))}(1 - e^{-V_{DS}/V_T})$;

PMOS: $\beta_p = \mu_p C_{ox}(W/L)$; $V_{tp} < 0$; $V_{DS} \leq 0$; (triode) $I_D = \beta_p((V_{GS} - V_{tp})V_{DS} - (V_{DS}^2/2))$; (active) $I_D = 0.5\beta_p(V_{GS} - V_{tp})^2$;
(triode) $V_{DS} \geq (V_{GS} - V_{tp})$; (active) $V_{DS} \leq (V_{GS} - V_{tp})$;

Simple cap model: $C_g = C_{ox}WL$; if L_{min} ; $C_{gu} \equiv C_{ox}L_{min}$; $C_g = C_{gu}W$; $C_d = C_s = C_{du}W$;

CMOS inverter: $V_{TH} = (V_{DD} + V_{tp} + V_{tn}r)/(1 + r)$; $r = \sqrt{(\mu_n(W/L)_n)/(\mu_p(W/L)_p)}$;

RC delay est: $t_{dr} = t_{df} = 1.2\tau$; $\tau = R_{eq}C$; $R_{eqn} = 2.5/(\mu_n C_{ox}(W/L)_n(V_{DD} - V_{tn}))$; $R_{eqp} = 2.5/(\mu_p C_{ox}(W/L)_p(V_{DD} + V_{tp}))$;
$(W_p/W_n)_{opt} = \sqrt{\mu_n/\mu_p}$ **Unit delay est:** $t_{df2}/t_{df1} = (C_{L2}/C_{L1}) \times ((W/L)_{n1}/(W/L)_{n2})$

Min delay: $t_{delay} = \tau_{inv}(C_{out}/C_{in})$; $\text{total}_{delay} = Nf\tau_{inv}$; $f^N = C_{out}/C_{in}$; usually $f = 4$

Power diss: $P_{dyn} = P_{1\to 0} f C_L V_{DD}^2$; $P_{dp} = 0.5 P_{1\to 0} f V_{DD} I_{peak}(t_r + t_f)$; $I_{peak} = 0.5\beta_n(V_{TH} - V_{tn})^2$;

Elmore Delay: $\tau_i \cong \sum_k C_k R_{ik}$; dist RC, $\tau \cong RC/2$;

Interconnect: $R = (\rho l)/(tw)$; $R_\square = \rho/t$; $C = (\varepsilon_{ox} wl)/t$; $C = \varepsilon_{ox} l(w/h + 0.77 + 1.06(w/h)^{0.25} + 1.06(t/h)^{0.5})$;

Max delay constraint: $T_c \geq t_{pcq} + t_{pd} + t_{setup}$ **Min Delay constraint:** $t_{hold} \leq t_{ccq} + t_{cd}$ **Metastability:** $\mathrm{MTBF} = e^{T/\tau_s}/(t_{rd} F_D F_{CLK})$

SRAM: M3 is cell access transistor, M1 is inverter NMOS, M5 is inverter PMOS,

SRAM read: $W_1/W_3 \geq (V_{DD} - V_A - V_{tn})^2/(2((V_{DD} - V_{tn})V_A - V_A^2/2))$; $I_{cell} = ((\mu_n C_{ox})/2)(W_3/L)(V_{DD} - 2V_{tn})^2$
$\Delta V_{BL} = (I_{cell}\Delta t)/C_{BL}$

SRAM write: $W_3/W_5 \geq (\mu_p(V_{DD} + V_{tp})^2)/(2\mu_n((V_{DD} - V_{tn})V_A - V_A^2/2))$